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NMR EVIDENCE FOR INHOMOGENEOUS GLASSY BEHAVIOR DRIVEN BY NEMATIC FLUCTUATIONS IN IRON ARSENIDE SUPERCONDUCTORS

We present ⁷⁵As nuclear magnetic resonance spin-lattice and spinspin relaxation rate data in $Ba(Fe_1-xCox)_2As_2$ and $Ba(Fe_1-xCux)_2As_2$ as a function of temperature, doping and magnetic field. The relaxation curves exhibit a broad distribution of relaxation rates, consistent with inhomogeneous glassy behavior up to 100 K. The doping and temperature response of the width of the dynamical heterogeneity is similar to that of the nematic susceptibility measured by elastoresistance measurements. We argue that quenched random fields which couple to the nematic order give rise to a nematic glass that is reflected in the spin dynamics.

Keywords: nuclear magnetic resonance, spin-lattice and spin-spin relaxation rate data, inhomogeneous glassy.

INTRODUCTION

The iron arsenide superconductors exhibit multiple phase transitions upon doping, including antiferromagnetism, unconventional superconductivity, and electronically-driven nematic ordering that breaks C4 rotation symmetry [1]. In the context of crystalline materials, nematic order refers to an orthorhombic lattice distortion that is driven by electronic rather than structural degrees of freedom [2]. In the iron pnictides, the transport anisotropy far exceeds the orthorhombicity, suggesting that the origin is electronic [3]. The orthorhombic, or nematic, phase is characterized by the presence of perpendicular twin domains [4]. Importantly, there is a strong coupling between the spin and orbital degrees of freedom ensuring that the antiferromagnetically ordered Fe spins lie along either of these two orthogonal directions [5]. Upon doping, the nematic and antiferromagnetic ordering temperatures are suppressed, yet strong antiferromagnetic fluctuations persist in the paramagnetic state beyond optimal doping, even in the absence of long range order [6]. Direct transport measurements of the electronic nematicity versus strain have uncovered a divergent nematic susceptibility in the paramagnetic phase [7]. The large nematic susceptibility necessarily implies the presence of nematic fluctuations in the disordered paramagnetic phase.

Nuclear magnetic resonance (NMR) has played a central role in the investigation of spin fluctuations in the iron arsenide superconductors. The ⁷⁵As nuclei (I = 3/2, 100 % abundant) experience a strong hyperfine coupling to the neighboring Fe spins [8], thus the spin lattice relaxation rate, T_1^{-1} , is a sensitive probe of the dynamical spin susceptibility of the Fe spins [9]. In the paramagnetic state of a homogeneous material, critical spin fluctuations exhibit a characteristic time scale, τc , that diverges as a power law at the phase transition temperature, $\tau c \propto (T - TN)^{-\alpha}$. Consequently, the NMR relaxation rate $T_1^{-1} \propto \tau c$ exhibits a sharp divergence at TN. NMR studies of T_1^{-1} in Ba(Fe₁–_xCo_x)₂As₂ and BaFe₂(As₁–xPx)₂ revealed the presence of spin fluctuations over a broad range of doping and temperature, with a quantum phase transition at a critical doping level, xc, that lies close to the maximal Tc [6,10,11].

Several recent experimental studies have reported a deviation from the expected power law divergence of T1⁻¹ as well as stretched exponential behavior. In LaFeAsO₁-xFx, Ba(Fe₁-xRhx)₂As₂, and Ba(Fe₁-xCox)₂As₂, the characteristic time scale of the antiferromagnetic fluctuations grows progressively slower over a broad temperature range, the spin-lattice recovery function exhibits stretched exponential behavior, and the NMR signal intensity is suppressed (wipeout) [12-15]. In the case of Ba(Fe₁-xCox)₂As₂, T1⁻¹ also changes character in the nematic state, diverging with a critical exponent $\delta \Box_{\frac{1}{2}}^{\frac{1}{2}}$ [11]. NMR studies at the ⁵⁹Co site reveal much weaker spin fluctuations near the magnetic transition [16,17], and ⁶³Cu site-selective NMR shows a similar local suppression of the spin fluctuations on the ⁶³Cu site and neighboring ⁷⁵As sites in addition to wipeout the NMR signal [18].

These features point to dynamical inhomogeneity, a characteristic of disordered spin glasses indicative of a distribution of relaxation rates, in which some fraction of the nuclei relax too quickly to be observed [19, 20]. Similar behavior has been observed in the cluster spin-glass phase of the underdoped high Tc cuprates [21-23], and charge ordering was discovered to be intimately related to the ⁷⁵As and ¹³⁹La NQR wipeout in the cuprates [22, 24]. The cuprates, however,

are doped Mott insulators, and the glassy behavior was attributed to intrinsic frustration between the competing effects of Coulomb repulsion and charge segregation [25, 26]. The iron arsenides do not exhibit charge ordering and thus a different mechanism must be driving the glassy dynamics. In order to investigate the glassy behavior in more detail, we have conducted detailed field, temperature and doping dependent studies of both the spin-lattice relaxation rate, T_1^{-1} , and the spin-spin decoherence rate, T_2^{-1} . We extract the temperature dependence of the correlation time, τc , and find that it can be described by Vogel-Fulcher behavior. We argue that the dynamical heterogeneity arises because the dopants introduce quenched random fields coupling to the nematic order. This disorder-induced frustration plays a significant role in suppressing antiferromagnetism and in the emergence of superconductivity.



Figure $1 - {}^{75}As$ spectra versus temperature for two different doping levels in Ba(Fe₁-xCox)₂As₂ measured by sweeping frequency at a constant field of 11.7 T and acquiring echoes for the field oriented perpendicular to the *c* axis. The spectra have been normalized to have equal intensities for comparison.

MAIN PART

Relaxation measurements. Single crystals of $Ba(Fe_1-xCox)_2As_2$ and $Ba(Fe_1-xCux)_2As_2$ were grown from a FeAs self-flux and the dopant concentrations were determined via wavelength dispersive X-ray spectroscopy (WDS) as described in Ref. [27]. Multiple WDS measurements were made for each batch, and the error bars on the concentrations are given by twice the standard deviation of these measurements. ⁷⁵As (100 % abundant, I = 3/2) NMR spectra, spin lattice relaxation, and spin echo decays were measured at the central transition ($Iz = \pm 1/2$) in several different applied fields oriented perpendicular to the c axis by acquiring spin echoes using standard pulse sequences. Fig. 1 shows representative spectra for two different doping levels as a function of temperature.

Relaxation rate distribution. In order to quantify the distribution of relaxation rates, we fit the ⁷⁵As magnetization recovery to a distribution: $M(t) = \int P(WI)f(W_1t)dWI$, where P(WI) describes the relaxation rate distribution, and the relaxation function f(x) is described below. For a homogeneous system P(WI) is a delta function centered at T_1^{-1} and thus $M(t) \Box f(t/T_1)$. If the distribution has a finite width, then the recovery function is more complex, typically exhibiting stretched behavior. For example, if the relaxation function $f(x) = e^{-x}$, then $M(t) \Box e^{-(t/TI)\beta}$, where $\beta \le 1$ is the stretching exponent [19]. Previous studies have reported stretched recovery, however the distribution for general β can only be expressed as an infinite series. Here we assume a log-normal distribution recovery directly. This form was chosen because it mimics the distribution for a stretched exponential recovery. This approach enables us to extract the width of the dynamical distribution of the nuclei that contribute to the NMR signal, a quantity that sheds important light on the glassy behavior.

A representative recovery data set with the best fit is shown in Fig. 2.



Figure 2 – Magnetization versus recovery time for the ⁷⁵As in Ba(Fe₁– $xCox)_2As_2$ with x = 0.062 at 30K. The solid line is the best fit using the protocol described in the text, and the dashed and dotted lines are the recovery curves assuming a stretched exponential (as described in Ref. 14) or a single relaxation time, respectively

The distribution function is given by:

$$P(W_1) = \frac{1}{W_1 \sigma \sqrt{2\pi}} e^{-\frac{1}{2} \left(\frac{\ln W_1 - \mu}{\sigma} \right)^2},$$
 (1)



Figure 3 – (a) Temperature dependence of $P(W_i)$ (normalized by peak height for clarity) and the median ⁷⁵As spin-lattice relaxation rate, T_1^{-1} , (markers) for Co-doping with x = 0.062 for $H_0 \parallel ab$. Here $T_1^{-1} = e^{\circ}$ is the median of the distribution, $P(W_i)$, as described in the text

The probability distribution broadens as temperature is decreased below $\Box 100$ K. Note the bottom axis is a log scale; the skewness of the Log-Normal distribution results in the median falling on the high side of the peak (mode). (b) T1⁻¹ for several Co concentrations as a function of temperature. (c) Standard deviation $\sigma_1 = \sqrt{\langle W_1^2 \rangle - \langle W_1 \rangle^2}$ of the distribution P(W1) for the same samples as a function of temperature in the normal state. Dashed lines in all subfigures indicate structural transition/nematic ordering temperature via bulk measurements reproduced from the literature [18,27-30].



Figure 4 – Temperature dependence of $P(W_i)$ (normalized by peak height for clarity) and the median ⁷⁵As spin-lattice relaxation rate, T_1^{-1} , (markers) for Co-doping with x = 0.062 for $H_0 \parallel ab$. The data is identical to that in Fig. 3(a), but is plotted on a linear scale

Recovery function for a spin 3/2 nucleus at the central transition is:

$$f(x) = M_0 \left[1 - 2\phi \left(\frac{9}{10} e^{-\delta x} + \frac{1}{10} e^{-x} \right) \right],$$
(2)

where $x = W_1 t$, t is the time between the initial inverting (or saturating) pulse and the spin echo which samples the nuclear magnetization, M0 is the equilibrium nuclear magnetization and M₀ is the inversion fraction. M(t) was numerically integrated during fitting using an adaptive Gaussian quadrature method and recalculated iteratively using a least squares method. The limits for the numerical integration were chosen to be 10⁻⁶s and 10⁶s, though choosing a smaller range when σ is small results in faster convergence. This choice of limits was made based on the timescale of the NMR experiment. Spins that relax faster or slower than this time window will not participate in the spin echo, and therefore provide natural limits of integration. The solid line in Fig. 2 shows the best fit determined in this fashion, as well as the best fits assuming either a stretched exponential, or a single value of T₁⁻¹ using Eq. 2. It is clear that a single uniform relaxation rate does not accurately describe the data, but both the stretched exponential and the distribution fit well.

Figs. 3(a) and 4 show the temperature dependence of the distribution $P(W_1)$, T_1^{-1} , and σ_1 as a function of temperature for Ba(Fe₁-xCox)₂As₂. The data reveal a progressive broadening of the distribution below 100K, as well as an increase in both T_1^{-1} and σ_1 reaching a peak at a temperature that coincides with the onset of long-range antiferromagnetic order at TN. The peak temperature is strongly doping dependent, reflecting the suppression of TN with doping concentration. The width σ_1 increases by two orders of magnitude, and is also doping dependent. This quantity is a direct measure of the degree of dynamical inhomogeneity of the system. Note that at low temperatures it is likely that the true width is even larger, but we are unable to capture the full distribution due to signal wipeout. A previous NMR study revealed that Ba(Fe₁-xCox)₂As₂ forms a cluster spin-glass state at low temperature below TN, characterized by a distribution of frozen antiferromagnetic domains coexisting with superconductivity [14]. Subsequent neutron scattering work concluded that this cluster spin-glass (or as termed by Lu et al. «moment amplitude spin glass») state emerges also in Ba(Fe₁-xNix)₂As₂ [31]. The NMR data, however indicate that this inhomogeneity begins to form at \Box 100 K, well above TN, where the spins are fluctuating dynamically. This large onset temperature suggests that the inhomogeneous fluctuations are unrelated to the presence of superconductivity, which emerges only below TN. Furthermore, if the glassy behavior arises strictly from disorder and frustration among the spin exchange interactions, it is surprising that the inhomogeneity would emerge at temperatures well above TN, where the spin presumably remain uncoupled.

Field and doping dependence. In order to explore the glassy behavior in more detail, we have carried out detailed studies of the field and temperature dependence of $P(W_1)$ as a function of doping in both superconducting and non-superconducting samples. Changing the magnetic field alters the Larmor frequency, enabling one to probe the frequency dependence of the slow dynamics. We measured the relaxation in both Ba(Fe₁-xCox)₂As₂ (up to 30.4 T at the National High Magnetic Field Laboratory) and Ba(Fe₁-xCux)₂As₂ (up to 8.75 T).



Figure 5 – Field and temperature dependence of the median (T_1^{-1}) and standard deviation (σ_1) of the distribution of ⁷⁵As relaxation rates for Co- and Cu-doped BaFe₂As₂. The peak in T_1^{-1} is strongly field dependent, typical for glassy dynamics. σ_1 grows substantially (~ 10⁴ s⁻¹) below 100 K, reflecting the inhomogeneous relaxation of the nuclei. Dashed lines indicate structural transition temperatures via bulk measurements reproduced from the literature [18, 27-30]

Fig. 5 shows T1⁻¹ for several different doping concentrations and fields as a function of temperature in Ba(Fe₁-xCox)₂As₂and Ba(Fe1-xCux)₂As₂. Both Co and Cu dopants suppress the long range nematic and antiferromagnetic ordering, but Cu also suppresses superconductivity to a maximum Tc ≈ 2 K, whereas Tc reaches a maximum of 23 K in Co-doped samples [1, 30]. This enables us to discern whether the glassy behavior is connected to the competing superconducting and antiferromagnetic ground states [32]. Both systems exhibit qualitatively similar glassy behavior, suggesting that its origin is unrelated to the superconductivity. The maximum T1⁻¹ is suppressed with field, reflecting the fact that the relaxation measurement is sampling the fluctuation spectrum at a different Larmor frequency. For a hyperfine field h(t), the autocorrelation function is given by $\langle h(t)h(0) \rangle = h_0^2 e^{-t/\tau_c}$, where h_0 is the root mean square value of the field and τc is the autocorrelation time [33]. In this case, the nuclear spin-lattice relaxation rate is:

$$W_1^{-1} = \frac{\gamma^2 h_0^2 \tau_c}{1 + \omega_l^2 \tau_c^2},$$
(3)

where $\gamma = 7.2919$ MHz/T is the ⁷⁵As gyromagnetic ratio and $\omega_L = \gamma H_0$ is the NMR Larmor frequency. Note that $P(W_1)$ reflects a distribution of both τ_c and h_0 . For concreteness, however, we consider only single values of these quantities giving rise to the median of the distribution, T_1^{-1} , which is an oversimplification for the real system. Eq. 3 shows that T_1^{-1} reaches a maximum when $\omega_L \tau_c = 1$ and is equal to T_1^{-1} , max = $\gamma h_0^2/2H_0$. Fig. 6 (a) shows T_1^{-1} , max varies linearly with H_0^{-1} for various dopings, as expected. The slope of this line gives h_0 (fit values given in Table 1), which decreases with dopant concentration, and agrees with previous measurements in LaFeAsO₁–xFx [12].

Table 1 – Fit parameters extracted for linear fits to $T_1^{-1,max}(H_0^{-1})$

Dopant	Doping x	h_0 (mT)	offset (s^{-1})
Co	0.058	7.04 ± 0.43	117.32 ± 24.50
Co	0.062	4.13 ± 0.34	90.28 ± 11.60
Cu	0.040	4.89 ± 0.07	48.02 ± 2.77

Using the measured h_0 , we proceed to extract τ_c . Solving Eqn. 3 for _c yields:

$$\tau_{c} = \omega_{L}^{-1} \left[\frac{T_{1,\max}^{-1}}{T_{1}^{-1}} \pm \sqrt{\left(\frac{T_{1,\max}^{-1}}{T_{1}^{-1}}\right)^{2} - 1} \right], \tag{4}$$

where the positive sign for the radical arises at low temperature below T1-1,max where $\tau c \Box \omega L = 1$, and the negative sign arises at high temperatures when $\tau c \Box \omega L = 1$. Fig.6 (b) presents an Arrhenius plot of $\tau c/\tau c0$ versus T-1, where $\tau c0$ is the high temperature limit of the correlation time. The data clearly deviate from linearity, indicating that there is not a single activation energy that describes the system. The solid black line represents a Vogel-Fulcher-Tamman law $(\tau c/\tau c0 = \exp(DTK/(T - TK)))$, with D = 0.5(4) and TK = 25(3)K). This behavior is often found in glassy systems, and indicates a 'fragile' glass, in which the effective activation energy increases with decreasing temperature reflecting the collective nature of the fluctuations [34]. TK represents the temperature below which the system becomes trapped in a local minimum in free energy at a glass transition temperature. In this case, TK appears to correspond roughly with the Neel temperature. However, based on constant field Co-doping variation fits, this trend appears to break down once TN(NMR) < Tc, where TN(NMR) is the temperature at which T_{1-1} reaches a maximum. Below this temperature, the spins are ordered in frozen clusters with a broad distribution of sizes [14,31]. For the Cudoped system, the τc exhibits more Arrhenius-type behavior. At x = 0.04, the peak 36

temperature of T1–1 is ≈ 20 K, which agrees with the phase diagram determined via bulk transport and magnetization [30]. It is unclear why the Cu-doped samples differ, but the data suggest that the fluctuations are less correlated in this system, which may, in turn, be related to the strong suppression of the superconductivity in this compound. Recent 63Cu NMR data suggest a strong local effect of the dopants, supporting such an interpretation [18].

The data in Figs. 5 and 6(b) indicate that $P(W_1)$ is slightly modified by the field. In particular, the median fluctuation rate τ_c and the width σ_1 are suppressed by fields up to 30.4 T in the Co-doped sample and 8.75 T in the Cu-doped sample. These results suggest that in high fields the distribution of domain sizes is narrowing and shifting toward smaller domains. Note that because of the wipeout effects, these characterizations of the temperature dependence of the glassy behavior may not fully capture the behavior of the entire distribution. Since we are unable to detect large domains (with correspondingly large correlation times τ_c) due to wipeout, it is possible that the field alters the domain distribution in a manner that shifts the weight of the observed distribution towards smaller sizes. Superconductivity in the Co-doped samples is also strongly suppressed in these fields, which may alter somewhat the domain distribution [27].

Spin Echo Decay. Further evidence for glassy behavior is found in the temperature dependence of the ⁷⁵As spin-echo decay curves. In addition to the increase in τ_c/τ_{c0} and σ_1 , the NMR signal intensity gradually becomes suppressed and the character of the echo decay changes below 100 K. Fig.7(a) shows the echo intensity following a standard echo pulse sequence $(\frac{\pi}{2} - \tau - \pi - \tau)$ for Ba(Fe₁xCox), As, with x = 0.062. The intensity decreases with pulse spacing τ due to various decoherence effects, including fluctuations of the hyperfine field, h(t), over the course of the spin echo experiment. The data have been normalized by temperature to account for the Curie susceptibility of the nuclei, and clearly reveal the suppression of intensity (wipeout) with decreasing temperature [14]. As seen in Fig. 7(a), the character of the echo decay function crosses over from a Gaussian-dominated decay at high temperatures to exponential decay below \Box 100 K. This crossover is due to the growth of fast spin fluctuations, contributing a factor $e^{-2W_2\tau}$ to the echo decay, with $W_2 = \gamma^2 h_z^2 \tau_c$. Here h_z^2 is the root mean square of the hyperfine field parallel to H_0 , in contrast to h_0 in Eq. 3 which lies perpendicular to H_0 [33]. Since there is a distribution of correlation times _c as evident from the T_1^{-1} data, we fit the echo decay data with the same protocol involving a distribution of decoherence rates, W2. The data were fit to the function: $M(2\tau) = \int_0^\infty P(W_2)g(2\tau)dW_2$, where $g(2\tau) = M_0 e^{-(2\tau)^2/2T_{2G}^2} e^{-2W_2\tau}$. Here W_2 is the exponential component of the spin-spin relaxation rate due to spin-fluctuations, τ is the time separating the $\pi/2$ and π pulses of the spin echo sequence, and T_{2G} is 37

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the temperature independent Gaussian component of the spin-spin relaxation. At high temperatures the echo decay has a Gaussian form, which reflects the complex direct and indirect couplings between the like As nuclei. We do not expect this component to change with temperature, whereas the growth of spin fluctuations at low temperature will affect W2 [33,35]. Each temperature dependent data set was fit globally with a temperature-independent T_{2G} to achieve the best fit to all temperatures. This global analysis was confirmed by individually fitting the data set at each temperature, results of which show no trend in T_{2G} as a function of temperature.



Figure 6 – (a) T1–1,max versus H0–1 for x = 0.058 and x = 0.062 in Ba(Fe1–xCox)2As2 and x = 0.04 in Ba(Fe1–xCux)2As2. The slope of these data sets reveal the RMS hyperfine field values at the As site, and the fit coefficients are detailed in Table I. (b) Arrhenius plot of log($\tau c/\tau c0$) versus inverse temperature for several different fields for Co doping with x = 0.058 and Cu doping with x = 0.04. The solid black line shows a Vogel-Fulcher-Tamman function, as described in the text

The data in Fig. 7(f) shows $P(W_2)$, panels (b) and (d) show the median T_2^{-1} and panels (c) and (e) show the standard deviation σ_2 for several doping levels and dopants as a function of temperature. The temperature dependence of T_2^{-1} agrees qualitatively with the correlation times extracted from the T_1^{-1} data seen in Fig.6 (b). $T_2^{-1} = \gamma^2 h_l^2 \tau_c$, therefore we expect a monotonic increase of T_2^{-1} with decreasing temperature. Surprisingly, the width σ_2 of this distribution differs from σ_1 extracted from the spin-lattice relaxation data, and exhibits a downturn below TN. Note, however, that $P(W_2)$ is cut off at large W_2 by the finite detection window of the NMR experiment, which is the primary cause of signal wipeout [20]. As a result, the measured width σ_2 is reduced as the majority of the distribution shifts outside of the detection window at low temperature.

Discussion. *Missing signal.* It is clear from Fig. 7 that signal wipeout of up to 80 % is present, consistent with previous measurements of the spectral intensity in these samples, which raises the question of where the missing signal has gone [14]. The system is either dynamically or spectrally inhomogeneous. In our experiments we find no significant broadening of the spectra in the paramagnetic state, as shown in Fig. 1. It is possible that the distribution is such that a large fraction of the nuclei resonate outside of this window, but the internal field in the ordered state is small in this range of dopings and the spectral shift for this field orientation is minimal [36].



Figure 7 – Temperature and field dependence of ⁷⁵As echo decay for Co-and Cu-doped BaFe₂As₂. (a) Echo decay curves for x = 0.062, scaled by the nuclear Curie susceptibility. These data are fit (solid lines, see text for details) to extract the distribution of spin-spin relaxation rates, $P(W_2)$. The data were globally fit holding the Gaussian component constant as a function of temperature, and by employing the same log-normal distribution form to fit the exponential component. (b) The median (T_2^{-1}) and (c) standard deviation (σ_2) of the distribution versus temperature for several Co-doped samples. (d) T_2^{-1} (e) σ_2 versus temperature for the Cu-doped sample. (f) The distribution $P(W_2)$ and median T_2^{-1} (markers) versus temperature for x = 0.04 at 6.5 T for Ba(Fe₁–xCux)₂As₂

The spin lattice relaxation was measured at the peak of this resonance, and it is possible that not all of the nuclei were inverted by the radiofrequency pulses. It is more likely, however, that the missing signal arises from dynamical heterogeneity, given the broad distribution of relaxation rates that we observe. The missing signal in this case arises from nuclei that are located in an environment with a sufficiently long τ_c such that they recover to equilibrium before they can contribute to the spin-echo signal. It is important to note that the distributions shown in Fig. 3, 4 and 7 are representative only of the nuclei that are actually contributing to the

signal. In fact the true distributions are likely to be much broader than what we are able to measure, as a significant portion of the nuclei experience even faster relaxation rates.

Glassy nematic fluctuations. The inhomogeneous fluctuation distribution cannot be understood simply in terms of critical slowing down of the spin degrees of freedom. The spin fluctuations are not averaged out spatially, implying the existence of multiple local domains of characteristic size $\xi_{\Box}\tau_{c}$. Figure 8(a) summarizes the doping dependence of the width, $\sigma_{1}(x, T)$, of the inhomogeneous distribution, where σ_{1} is related to the distribution of domain sizes. For the parent compound BaFe₂As₂ we find that the recovery fits best to a single component of relaxation for all temperatures, so the system is dynamically homogeneous. σ_{1} remains small for the lightly Co-doped regime; however near optimal doping it becomes a strong function of temperature, reflecting a large dynamical inhomogeneity both in the Co and Cu-doped crystals.

A likely origin for this inhomogeneity is nematic fluctuations associated with the proximate tetragonal-to-orthorhombic structural phase transition. The doping and temperature trends exhibited by $\sigma_1(x, T)$ shown in Fig. 8(a) closely resemble the behavior of the static nematic susceptibility, χ_n .⁷³ Chu et al. have found that $\chi_n(T)$ exhibits Curie-Weiss behavior, with Weiss temperature θ that vanishes at the critical doping of xc = 0.07 for the Co-doped system. The fluctuation-dissipation theorem implies that because of the large susceptibility, there are also significant thermal fluctuations of the nematic order. In other words, even though there is no long-range nematic order, local orthorhombic distortions continue to fluctuate well above the ordering temperature. Because the spins are strongly coupled to the nematicity, these nematic fluctuations will drive spin fluctuations, which in turn couple to the nuclei via the hyperfine interaction to influence nuclear spin-lattice relaxation. In fact, T_1^{-1} scales with shear modulus in this phase, reflecting the fact that both quantities are probing the dynamics of the nematic fluctuations [37].

The glassy inhomogeneous nature of the fluctuations, therefore, probably reflects a property of the nematic fluctuations. Because the nematic order has Ising symmetry and breaks spatial symmetry, it is highly sensitive to quenched random impurities and is prone to exhibit glassy behavior [38]. The theory of electronic nematic order and the role of disorder is well established in the context of the cuprates [39-44], and more recently in the context of the iron pnictides [45,46]. The dopant atoms may provide a random field potential for nematic order that suppresses the phase transition temperature and gives rise to a distribution of frustrated nematic domains with different fluctuation rates, as illustrated in Fig. 8(b). With increasing dopant concentration, the nematic ordering transition is gradually suppressed. In the disordered phase, there are fluctuating patches in

which C4 symmetry is temporarily and locally broken, but there is no long range or static order. These fluctuating patches, however, exhibit a broad range of sizes and fluctuation times. The inhomogeneity we observe reflects the distribution of these patches. The NMR data indicate that the nematic fluctuations and distribution of domains persist up to \Box 100 K, as shown in Fig. 8(a). The local autocor-relation time of the domains, τ_c , is proportional to the domain size, thus the width of the distribution of domain sizes grows up to two orders of magnitude by the onset of long range nematic order. This scenario provides a natural explanation for the large χ_n as well as the broad distribution of relaxation times observed in our NMR experiments. Further, it explains the similarity of the phase diagram of both electron and hole-doped systems, as well as the isovalent BaFe₂(As₁–xPx)₂, system [10].



Figure 8 – (a) Temperature vs. doping phase diagram of Cuand Co-doped BaFe₂As₂. Markers have been reproduced from bulk measurements in the literature, and solid lines are a guide to the eye.^{18,27–30} The color scale overlay shows the standard deviation $\sigma_1 = \sqrt{\langle W_1^2 \rangle - \langle W_1 \rangle^2}$ for the distribution $P(W_p)$, characterizing the degree of inhomogeneity of the NMR spin-lattice relaxation rate. (b) Schematic of local nematic domains, indicating directions of Fe spin (arrows). The tetragonal and orthorhombic unit cell axes are shown. The local nematicity is oriented along the ellipses

The temperature-pressure phase diagram of the stoichiometric parent compound also exhibits a suppression of antiferromagnetism and emergence of

superconductivity without the presence of dopants [47, 48]; however, natural lattice defects may provide a source of quenched disorder that could be amplified by non-hydrostatic pressure.

On the other hand, non-isovalent dopants clearly play a role in tuning the density of states, as revealed by a recent study of simultaneous hole- and electrondoping in $Ba_1xKxFe_{1.86}Co_{0.14}As_2$ demonstrating that that the magnetic state can be partially recovered by compensating the carrier concentration [49]. Thus both disorder and tuning the density of states appear to be important parameters controlling the phase diagram.

CONCLUSION

In summary, the glassy behavior we observe in the dynamics reveal a highly inhomogeneous system in a region of the phase diagram that is nominally a homogeneous disordered paramagnetic phase. The NMR response probes the Fe spins through the hyperfine coupling, but it is the nematicity that drives the response of the system. The disorder introduced by the dopants generates random strain fields, which couple to the nematicity and may contribute to the suppression of the nematic ordering temperature. The nematic order parameter develops a complex fluctuating spatial landscape, with various domain sizes. Future measurements under uniaxial strain may significantly suppress the width of the distribution, and will provide an important avenue to investigate the dynamics in the glassy phase. NMR studies of the dynamics under pressures up to 10-15 GPa in stoichiometric samples will also help to elucidate the role of disorder in suppressing the nematic phase.

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REFERENCES

1 Canfield, P. C. and Bud'ko, S. L. Annu. Rev. Conden. Ma. P. 1, 27 (2010).

2 Fradkin, E., Kivelson, S. A., Lawler, M. J., Eisenstein, J. P. and Mackenzie, A. P. Annu. Rev. Conden. Ma. P. 1, 153. – 2010.

3 Chu, J.-H., Analytis, J. G., De Greve, K., McMahon, P. L., Islam, Z., Yamamoto, Y. and Fisher, I. R. Science 329, 824. – 2010.

4 Tanatar, M. A., Kreyssig, A., Nandi, S., Ni, N., Bud'ko, S. L., Canfield, P. C., Goldman, A. I. and Prozorov, R. Phys. Rev. B 79, 180508. – 2009.

5 Fernandes, R. M. and Schmalian, J. Supercond. Sci. Technol. 25, 084005. – 2012.

6 Ning, F. L., Ahilan, K., Imai, T., Sefat, A. S., McGuire, M. A., Sales, B. C., Mandrus, D., Cheng, P., Shen, B. and Wen, H.-H. Phys. Rev. Lett. 104, 037001. – 2010.

7 Chu, J.-H., Kuo, H.-H., Analytis, J. G. and Fisher, I. R. Science 337, 710. – 2012.

8 Kitagawa, K., Katayama, N., Ohgushi, K., Yoshida, M. and Takigawa, M. J. Phys. Soc. Jpn. 77, 114709. – 2008.

9 Smerald, A. and Shannon, N. Phys. Rev. B 84, 184437. - 2011.

10 Nakai, Y., Iye, T., Kitagawa, S., Ishida, K., Ikeda, H., Kasahara, S., Shishido, H., Shibauchi, T., Matsuda, Y. and Terashima, T. Phys. Rev. Lett. 105, 107003. – 2010.

11 Ning, F. L., Fu, M., Torchetti, D. A., Imai, T., Sefat, A. S., Cheng, P., Shen, B. and Wen, H.-H. Phys. Rev. B 89, 214511. – 2014.

12 Hammerath, F., Gräfe, U., Kühne, T., Kühne, H., Kuhns, P. L., Reyes, A. P., Lang, G., Wurmehl, S., Büchner, B., Carretta, P. and Grafe, H.-J. Phys. Rev. B 88, 104503. – 2013.

13 Bossoni, L., Carretta, P., Halperin, W. P., Oh, S., Reyes, A., Kuhns, P. and Canfield, P. C. Phys. Rev. B 88, 100503. – 2013.

14 Dioguardi, A. P., Crocker, J., Shockley, A. C., Lin, C. H., Shirer, K. R., Nisson, D. M., Lawson, M. M., apRoberts Warren, N., Canfield, P. C., Bud'ko, S. L., Ran, S. and Curro, N. J. Phys. Rev. Lett. 111, 207201. – 2013.

15 Grafe, H.-J., Gräfe, U., Dioguardi, A. P., Curro, N. J., Aswartham, S., Wurmehl, S. and Buchner, B. Phys. Rev. B 90, 09451. – 2014.

16 Ning, F., Ahilan, K., Imai, T., Sefat, A. S., Jin, R., McGuire, M. A., Sales, B. C. and Mandrus, D. J. Phys. Soc. Jpn. 77, 103705. – 2008.

17 Ning, F. L., Ahilan, K., Imai, T., Sefat, A. S., Jin, R., McGuire, M. A., Sales, B. C. and Mandrus, D. Phys. Rev. B 79, 140506. – 2009.

43

18 Takeda, H., Imai, T., Tachibana, M., Gaudet, J., Gaulin, B. D., Saparov, B. I. and Sefat, A. S. Phys. Rev. Lett. 113, 117001. – 2014.

19 Johnston, D. C. Phys. Rev. B 74, 184430. - 2006.

20 Curro, N., Hammel, P., Suh, B., Hücker, M., Büchner, B., Ammerahl, U. and Revcolevschi, A. Phys. Rev. Lett. 85, 642. – 2000.

21 Julien, M.-H., Campana, A., Rigamonti, A., Carretta, P., Borsa, F., Kuhns, P., Reyes, A. P., Moulton, W. G., Horvati 'c, M., Berthier, C., Vietkin, A. and Revcolevschi, A. Phys. Rev. B 63, 144508. – 2001.

22 Hunt, A., Singer, P., Thurber, K. and Imai, T. Phys. Rev. Lett. 82, 4300. – 1999.

23 Mitrovi'c, V. F., Julien, M.-H., de Vaulx, C., Horvati'c, M., Berthier, C., Suzuki, T. and Yamada, K. Phys. Rev. B 78, 014504. – 2008.

24 Hunt, A. W., Singer, P. M., Cederstr"om, A. F. and Imai, T. Phys. Rev. B 64, 134525. – 2001.

25 Schmalian, J. and Wolynes, P. G. Phys. Rev. Lett. 85, 836. – 2000.

26 Westfahl, H., Schmalian, J. and Wolynes, P. G. Phys. Rev. B 64, 174203. – 2001.

27 Ni, N., Tillman, M. E., Yan, J.-Q., Kracher, A., Hannahs, S. T., Bud'ko, S. L. and Canfield, P. C. Phys. Rev. B 78, 214515. – 2008.

28 Pratt, D. K., Kim, M. G., Kreyssig, A., Lee, Y. B., Tucker, G. S., Thaler, A., Tian, W., Zarestky, J. L., Bud'ko, S. L., Canfield, P. C., Harmon, B. N., Goldman, A. I. and McQueeney, R. J. Phys. Rev. Lett. 106, 257001. – 2011.

29 Chu, J.-H., Analytis, J. G., Kucharczyk, C. and Fisher, I. R. Phys. Rev. B 79, 014506. – 2009.

30 Ni, N., Thaler, A., Yan, J. Q., Kracher, A., Colombier, E., Bud'ko, S. L., Canfield, P. C. and Hannahs, S. T. Phys. Rev. B 82, 024519. – 2010.

31 Lu, X., Tam, D.W., Zhang, C., Luo, H., Wang, M., Zhang, R., Harriger, L.W., Keller, T., Keimer, B., Regnault, L.-P., Maier, T. A., and Dai, P. Phys. Rev. B 90, 024509. – 2014.

32 Nussinov, Z., Vekhter, I. and Balatsky, A. V. Phys. Rev. B 79, 165122. – 2009.

33 Slichter, C. P. Principles of Nuclear Magnetic Resonance, 3rd ed. – Springer-Verlag, 1992.

34 Berthier, L. and Biroli, G. Rev. Mod. Phys. 83, 587. – 2011.

35 Curro, N. and Slichter, C. J. Magn. Reson. 130, 186. – 1998.

36 Dioguardi, A. P., apRoberts Warren, N., Shockley, A. C., Bud'ko, S. L., Ni, N., Canfield, P. C., and Curro, N. J. Phys. Rev. B 82, 140411(R). – 2010.

37 Fernandes, R. M., B"ohmer, A. E., Meingast, C. and Schmalian, J. Phys. Rev. Lett. 111, 137001. – 2013.

38 Imry, Y. and Ma, S.-k. Phys. Rev. Lett. 35, 1399. – 1975.

39 Kivelson, S. A., Fradkin, E. and Emery, V. J. Nature 393, 550. – 1998.
 40 Carlson, E. W., Dahmen, K. A., Fradkin, E. and Kivelson, S. A. Phys
 Rev. Lett. 96, 097003. – 2006.

41 Carlson, E. W. and Dahmen, K. A. Nature Communications 2, 379. – 2010.
42 Xu, C., Müller, M., and Sachdev, S. Phys. Rev. B 78, 020501. – 2008.
43 Loh, E. W. Carlson, and Dahmen, K. A. Phys.Rev. B 81, 224207. – 2010.
44 Nie, L., Tarjus, G. and Kivelson, S. A. Proc. Natl. Acad. Sci. 111, 7980. – 2014.
45 Fang, C., Yao, H., Tsai, W.-F., Hu, J. and Kivelson, S. A. Phys. Rev.

B 77, 224509. - 2008.

46 Kuo, H.-H., Chu, J.-H., Kivelson, S. A., and Fisher, I. R. 1503.00402. – 2015. 47 Colombier, E., Bud'ko, S. L., Ni, N. and Canfield, P. C. Phys. Rev. B 79, 224518. – 2009.

48 Colombier, E., Torikachvili, M. S., Ni, N., Thaler, A., Bud'ko, S. L. and Canfield, P. C. Supercond. Sci. Technol. 23, 054003. – 2010.

49 Zinth, V., Dellmann, T., Klauss, H.-H. and Johrendt, D. Angew. Chem. Int. Ed. Engl. 50, 7919. – 2011.

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Темір арсениді асқын өткізгішінің нематикалық тербелістерімен шартталған бір текті емес шыны тәрізді тәртіптің ЯМР дәлелі

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ЯМР доказательства неоднородного стекловидного поведения, обусловленного нематическими колебаниями сверхпроводника арсенида железа

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Біз ⁷⁵As ядролық спин-торлық және спин-спиндік магниттік резонанының температурага, легирлеуге және магнит өрісіне байланысты Ba (Fe1-xCox) 2As₂ және Ba (Fe 1-xCox) 2As₂ релаксациясы жылдамдығы туралы мәліметтер ұсынамыз. Релаксация қисықтары бір текті емес шыны тәрізді тәртіпке сәйкес 100 К дейін релаксация жылдамдықтарының кең үлестірілуін демонстрациялайды. Легирлеу және динамикалық бір текті еместік енінің температурасынан тәуелділік, серпімді кедергіні өлшеу көмегімен өлшенген, нематикалық алғырлыққа ұқсас. Біз спиннің динамикасында көрініс тапқан, нематикалық шыны тудыратын, нематикалық тәртіпте бірігетін кездейсоқ өрістердің өшетіндігі туралы сендіріп айтамыз.

Мы представляем данные о скорости релаксации ⁷⁵As ядерного магнитного резонанса спин-решеточной и спин-спиновой в Ba (Fe1-xCo_x) 2As2 и Ba (Fe 1-xCox) 2As₂ в зависимости от температуры, легирования и магнитного поля. Кривые релаксации демонстрируют широкое распределение скоростей релаксации, в соответствии с неоднородным стекловидным поведением вплоть до 100 К. Легирование и зависимость от температуры ширины динамической неоднородности аналогично нематической восприимчивости, измеренной с помощью измерений упругого сопротивления. Мы утверждаем, что гасятся случайные поля, которые соединяются в нематическом порядке, порождающим нематическое стекло, что находит отражение в динамике спина. Теруге 15.09.16 ж. жіберілді. Басуға 18.09.2016 ж. қол қойылды. Пішімі 70х100 ¼₁₆. Кітап-журнал қағазы. Шартты баспа табағы 5,06. Таралымы 300 дана. Бағасы келісім бойынша. Компьютерде беттеген М. А. Шрейдер Корректорлар: А. Р. Омарова, Б. Б. Ракишева Тапсырыс № 2955

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